

Errors Resulting From Assuming Unconfined Aquifers Are Constant Thickness

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Please Understand

- Not yet published – preliminary
- Don't blame you if you are skeptical

The Problem

Common thinking is that if changes in aquifer thickness are a small proportion of total thickness (maybe 10%) then effects of assuming constant thickness are small

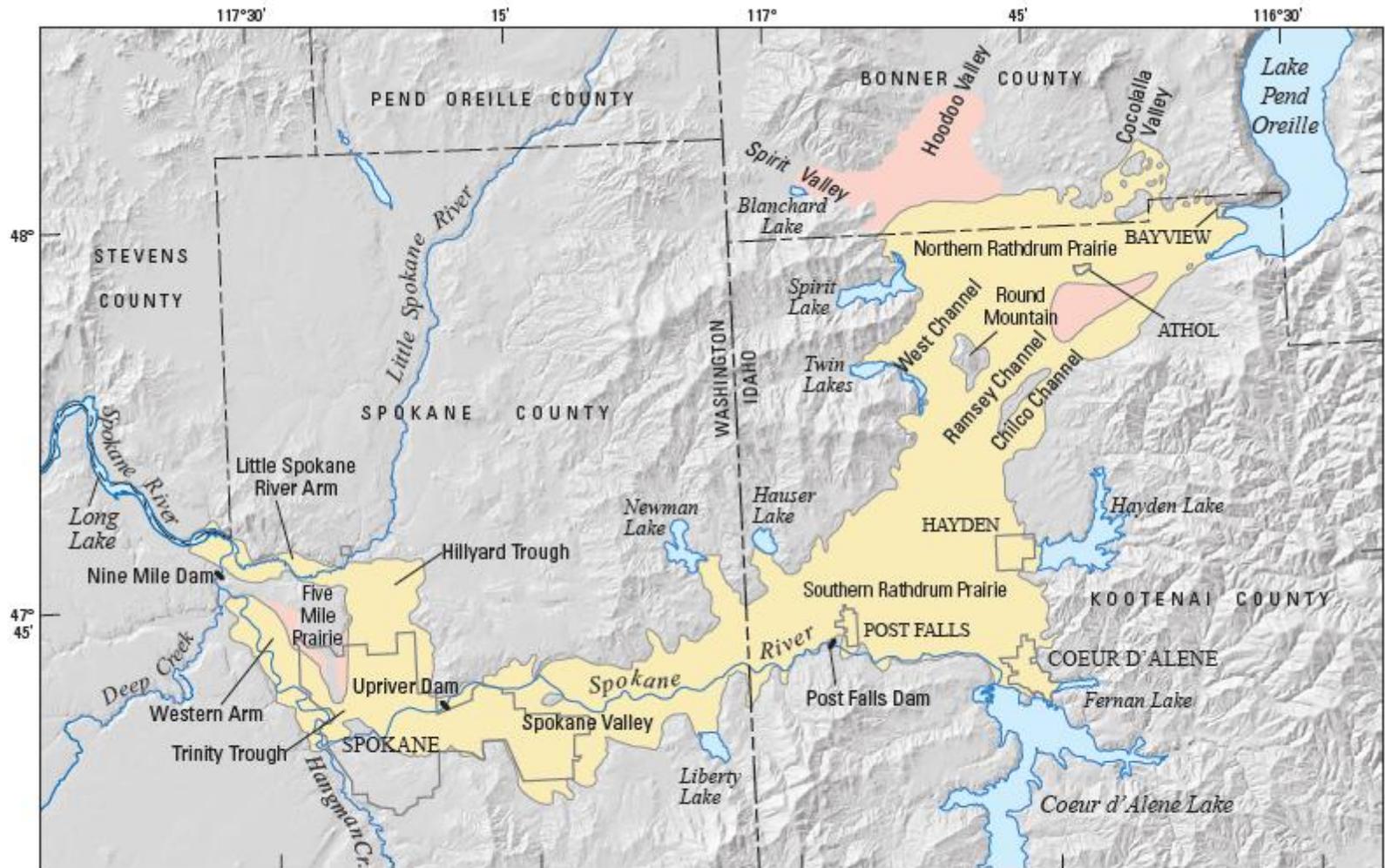
Not necessarily true when evaluating responses of surface water gains and losses relative to magnitude of imposed stress

STEP 1: Attempt to convince you that the second statement is true

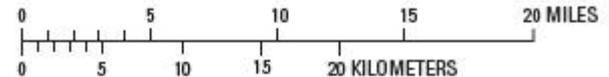
- SVRP model runs**
- Idealized model runs (not presented)**
- Analytical solutions (not presented)**

STEP 2: What does it mean for SRPA

SVRP Model Runs



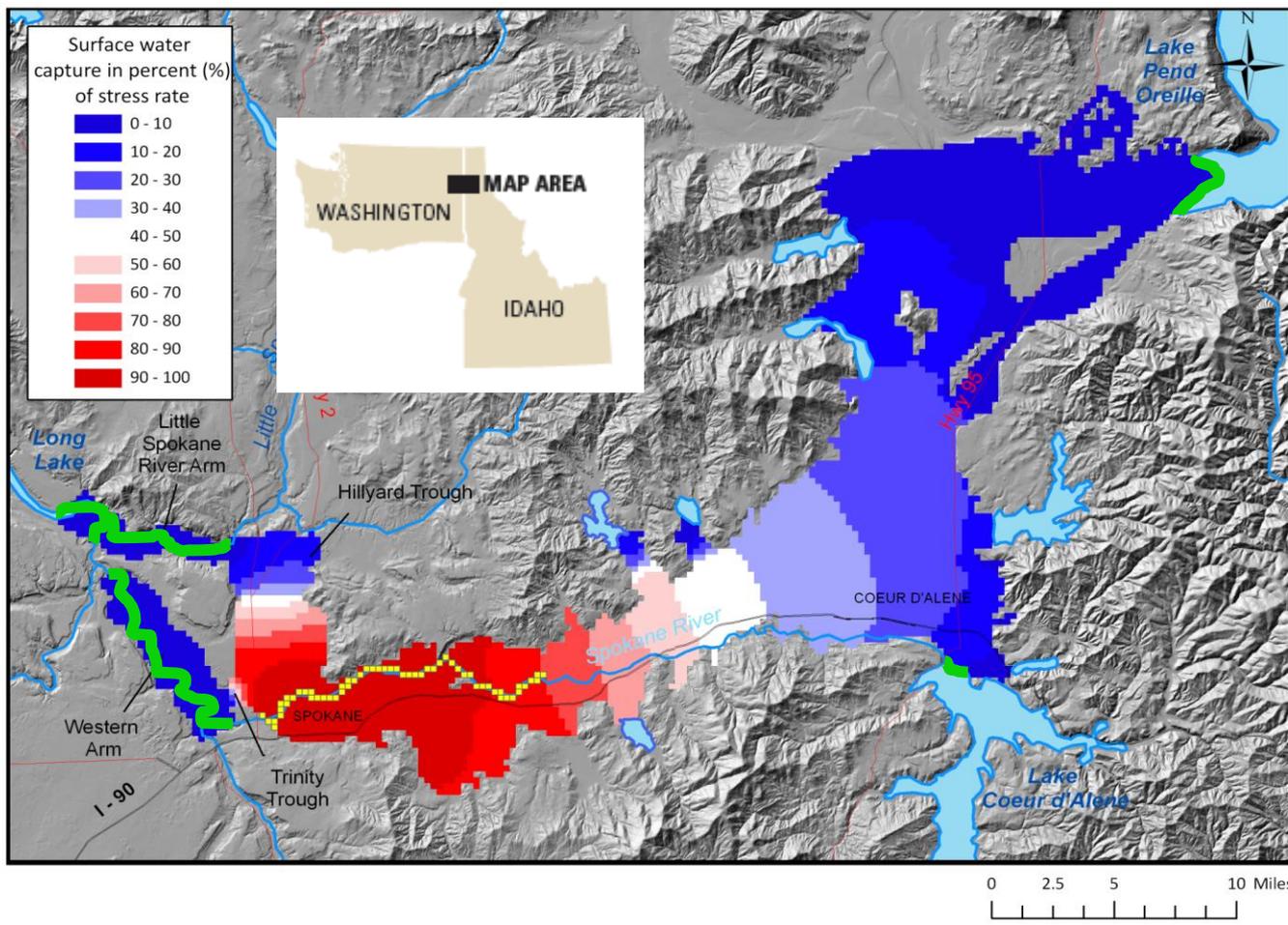
Base modified from U.S. Geological Survey digital data.
City boundaries, 1:24,000, various years (1961-86);
Public land survey, 1:100,000, 1985; Lakes, 1:100,000, 1995;
and rivers, 1:100,000, 1985. North American Datum of 1983 (NAD 83).



SVRP

- Unconfined except Hillyard Trough has deeper confined layer
- Calibrated as constant thickness then changed to unconfined representation
- Attempted response function generation with constant thickness and variable thickness representations – results showed areas of substantial difference
- Differences much greater than anticipated based on aquifer thickness

Reponses of Middle Segment of Spokane River



Linearity Evaluation

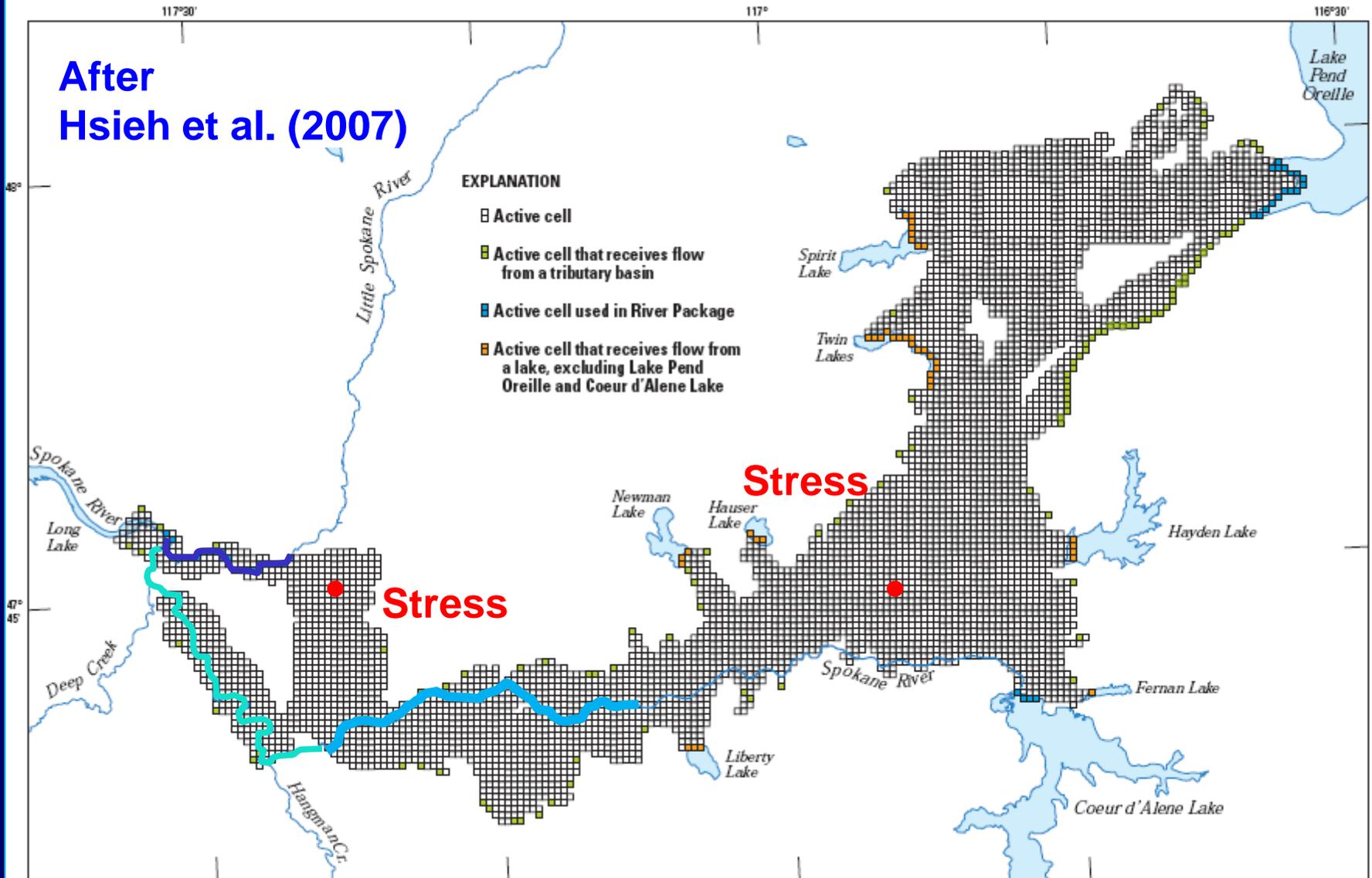
$$\text{Error} = \left(\begin{array}{c} \text{Unconfined} \\ \text{Response} \\ (\% \text{ of stress}) \end{array} \right) - \left(\begin{array}{c} \text{Confined} \\ \text{Response} \\ (\% \text{ of} \\ \text{stress}) \end{array} \right)$$

Confined response:

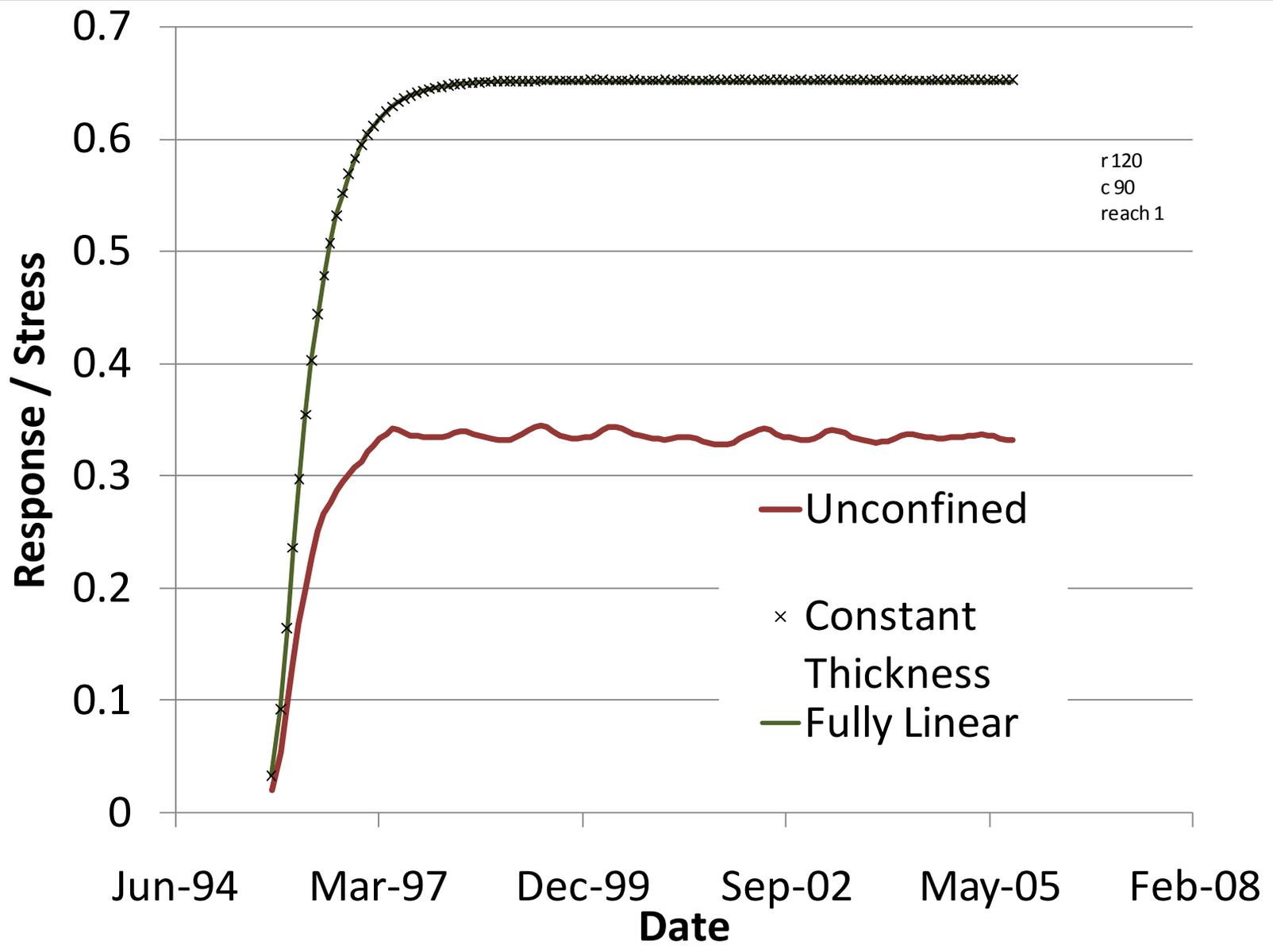
**constant thickness = average thickness from
same time period**

Spokane Valley Rathdrum Prairie Example

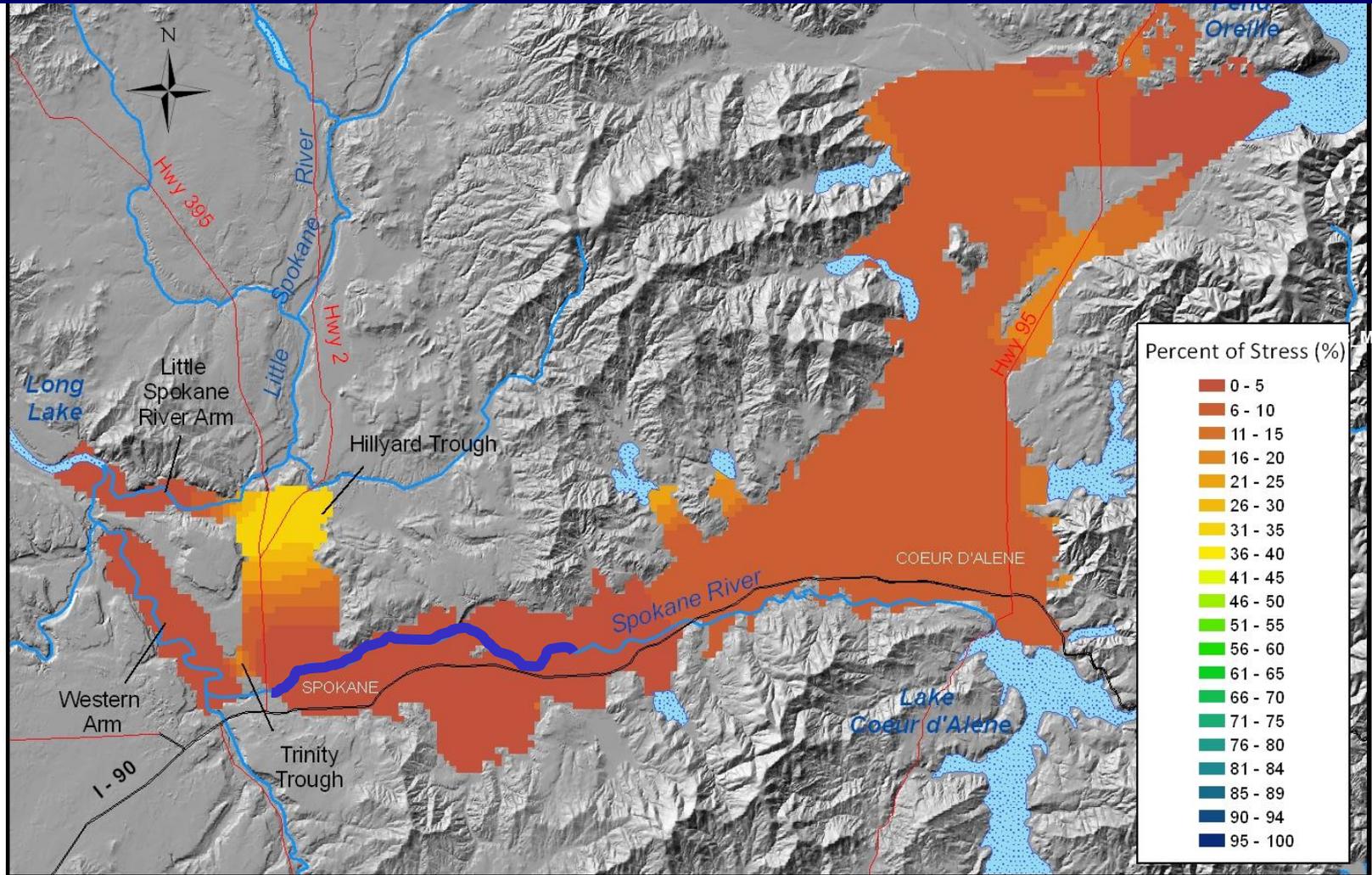
After
Hsieh et al. (2007)



Example Response Differences



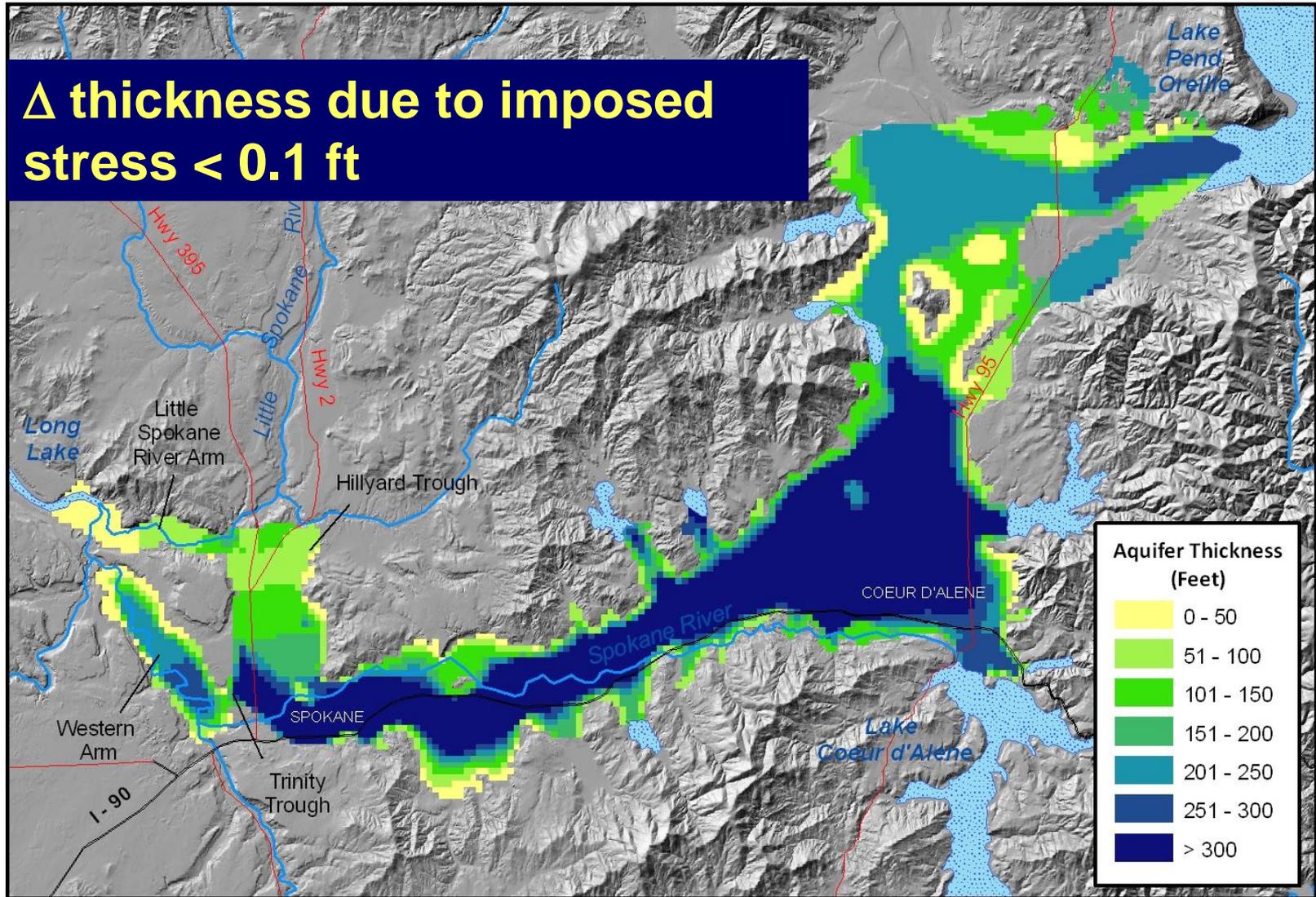
Map of Relative Error (percent of stress)



0 2.5 5 10 Miles

Aquifer Thickness Map

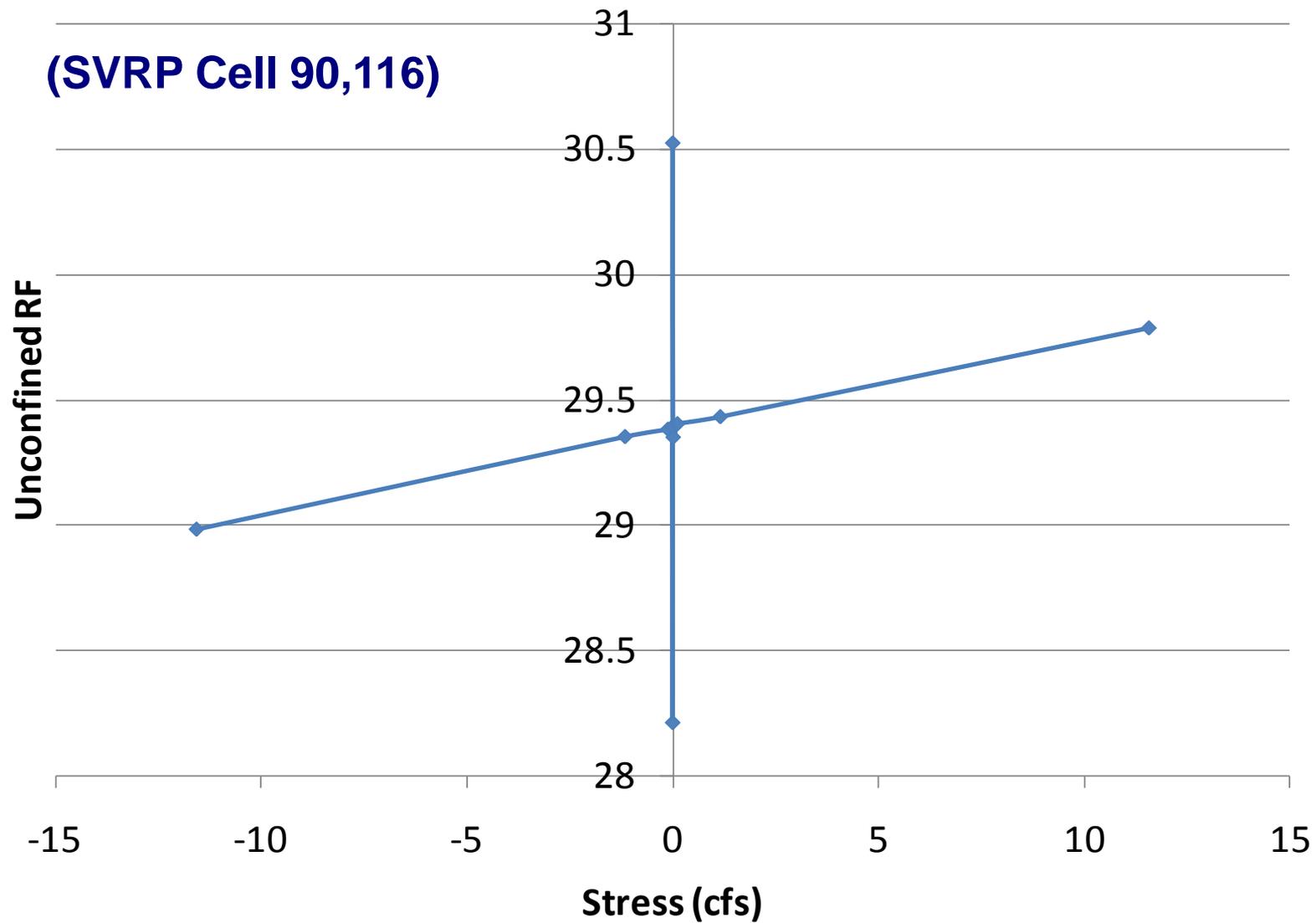
Δ thickness due to imposed stress < 0.1 ft



SVRP Summary

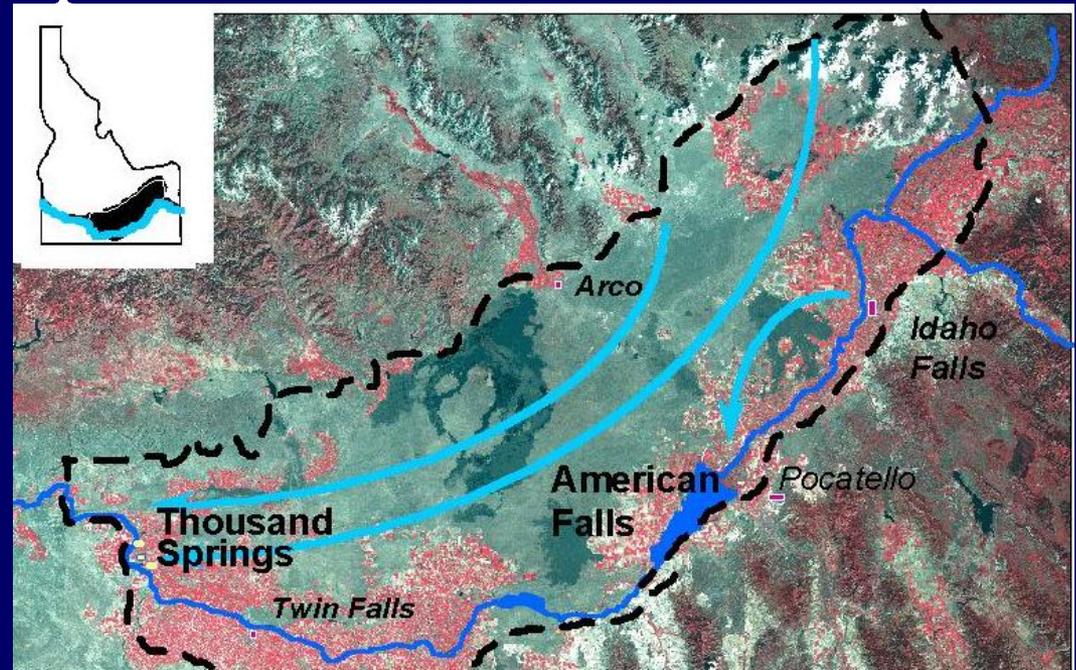
- Unexpectedly large errors from using constant thickness representation in some locations
- Change in thickness less than 1% of total thickness
- Variable thickness representation produces consistent responses regardless of stress magnitude (within limits) or sign
- Response function maps generated with variable thickness representation
- Also some (but more limited) errors due to treating boundaries as linear condition

Stress Magnitude Has Little Impact on RF

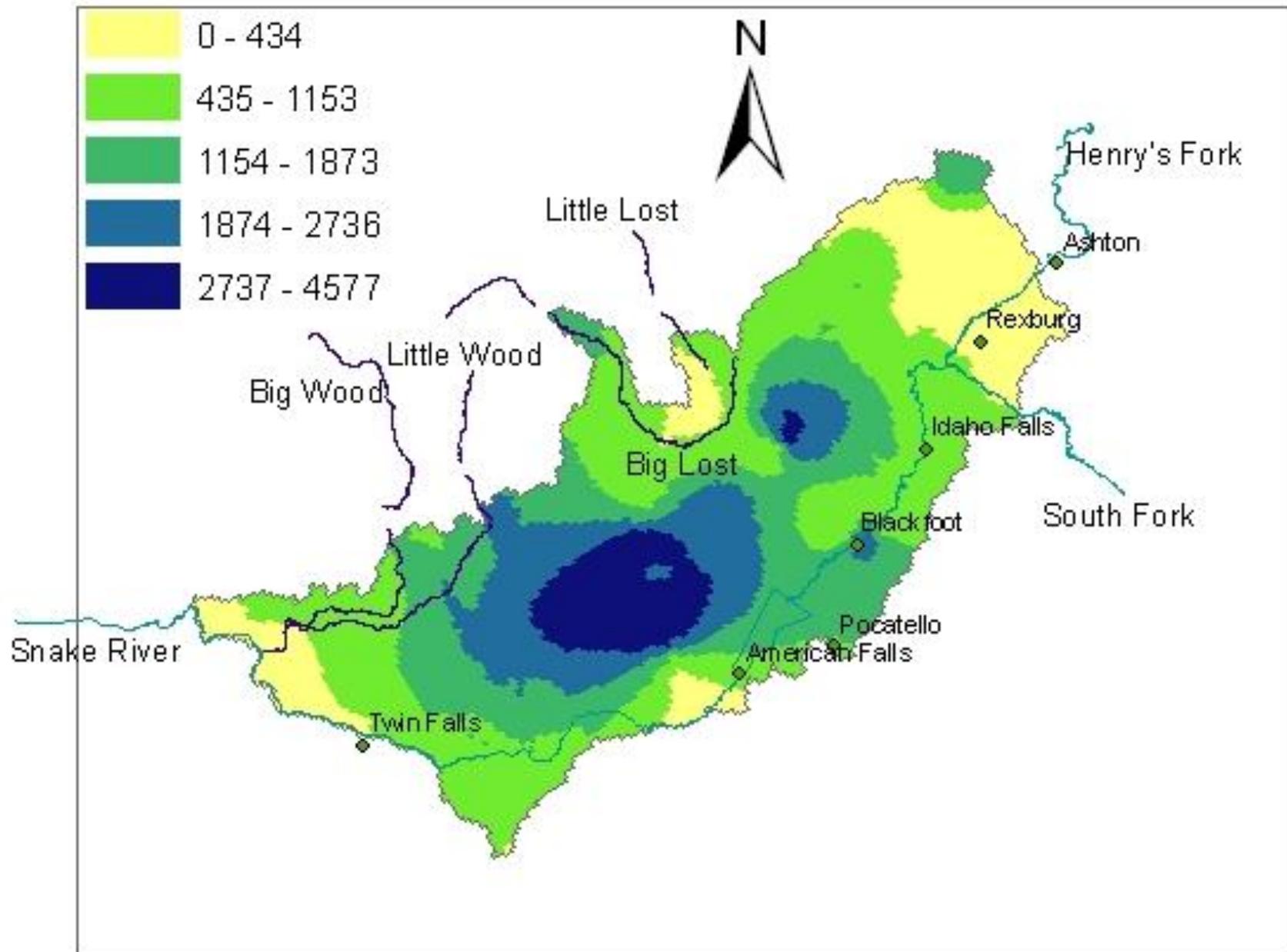


Implications: Snake River Plain

- Treated as constant thickness
- May be used for management simulations that examine effect of ground water pumping on surface water
- Need to evaluate impact of constant thickness assumption



Thickness in feet



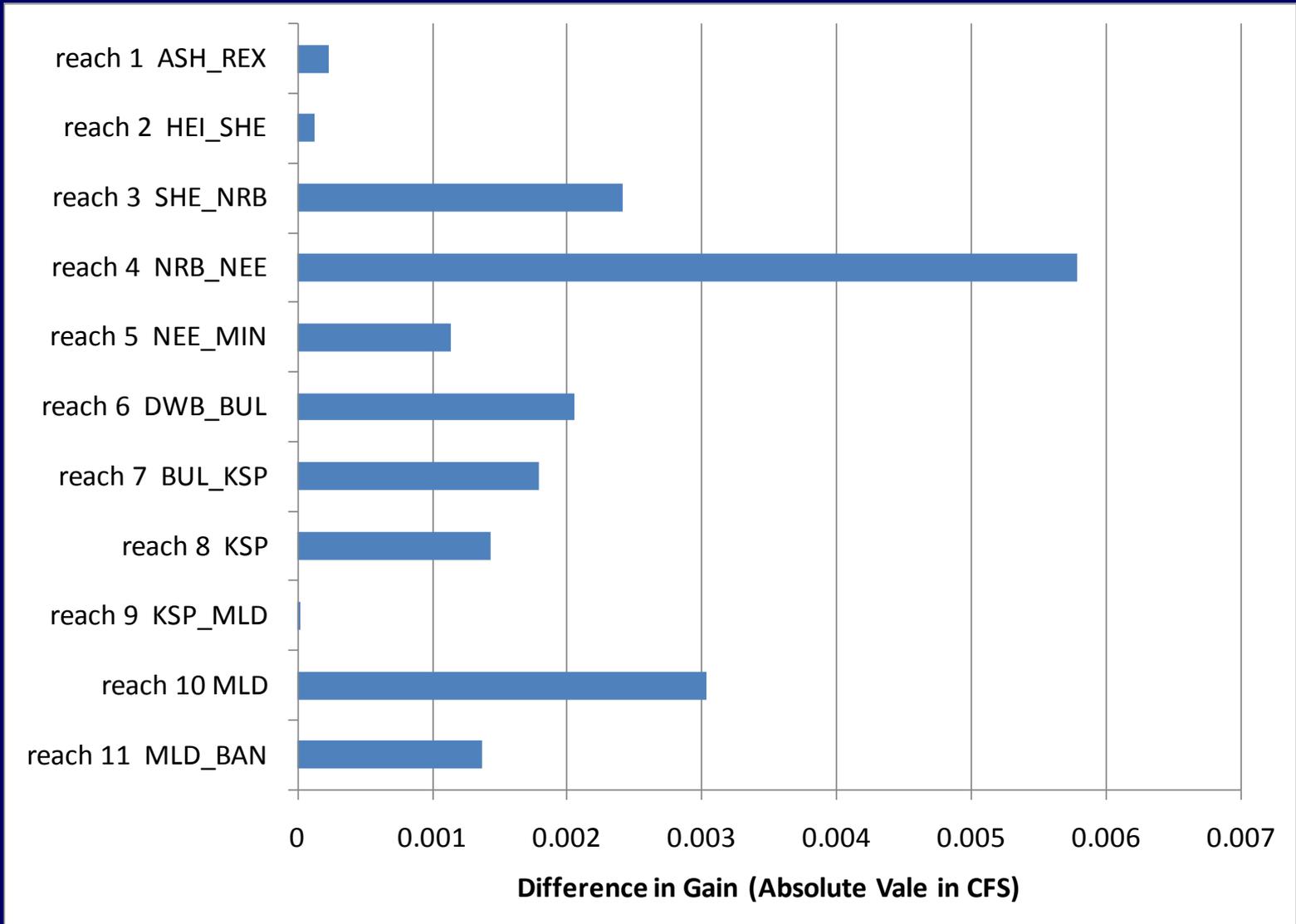
Snake Plain SS Constant Thickness (Confined) and Unconfined Simulations

- Used files from IDWR ftp site for SS SRPAM1.1
- Double precision MODFLOW version used
 - Required change to PCG solver
 - Required new post processing programs
 - Reduced mass balance error by over 2 orders of magnitude (less than 8 cfd for all simulations)

Procedure

- Original SS Confined simulation (DP)
- Determine thickness and calculate $K = T/b$ at each cell
- Data file changes as necessary (K for T)
- Unconfined SS simulation (DP)
 - Reach gains match confined pretty well (next slide)
- Stress each model cell at 11.57 cfs and difference reach gains from respective unstressed (confined or unconfined) and express as ratio to stress
- Difference unconfined and confined response ratios

Difference in Reach Gains Confined and Unconfined SS



Difference Maps

Stressed Unconfined
Reach Gain

UnStressed Unconfined
Reach Gain

RF(unconf) =

1000000

Stressed Confined
Reach Gain

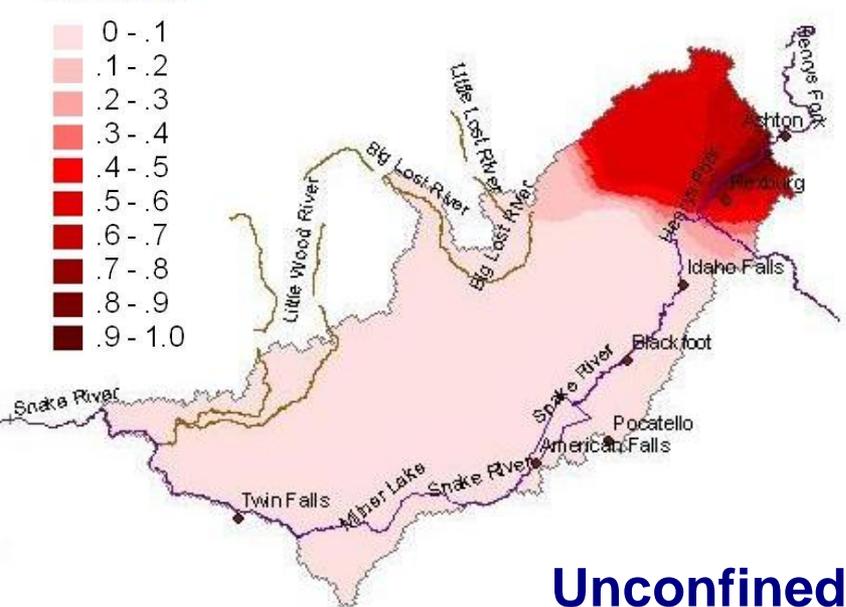
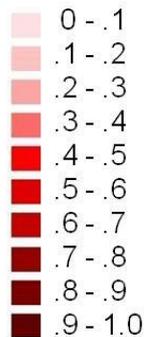
UnStressed Confined
Reach Gain

RF(conf) =

1000000

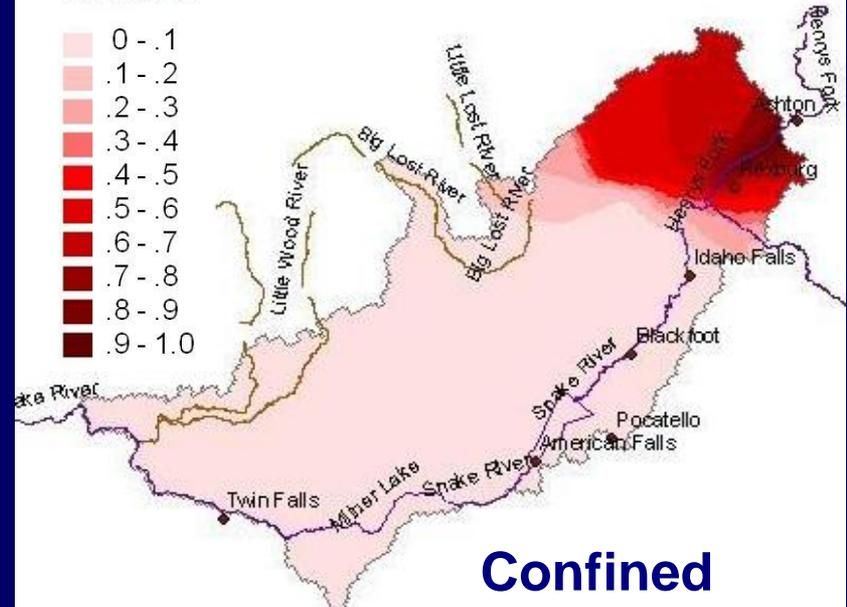
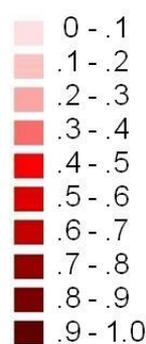
Difference = RF(unconf) – RF(conf)

Unconfed RF



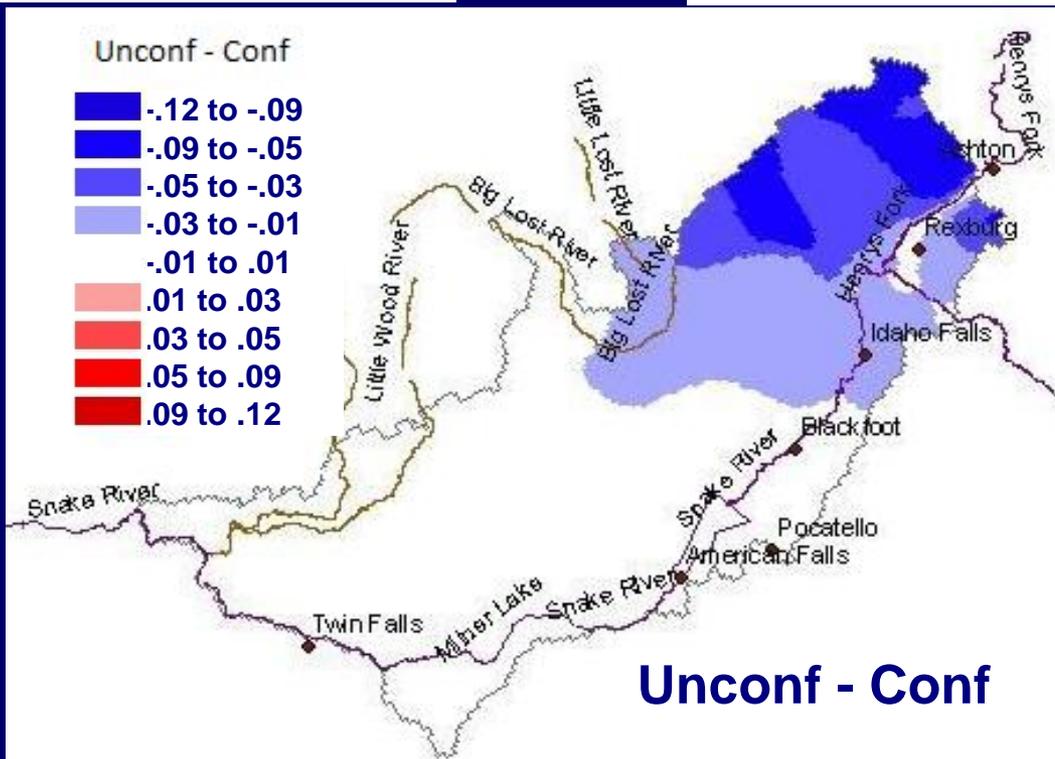
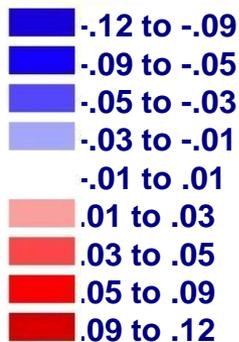
Unconfined

Confined RF



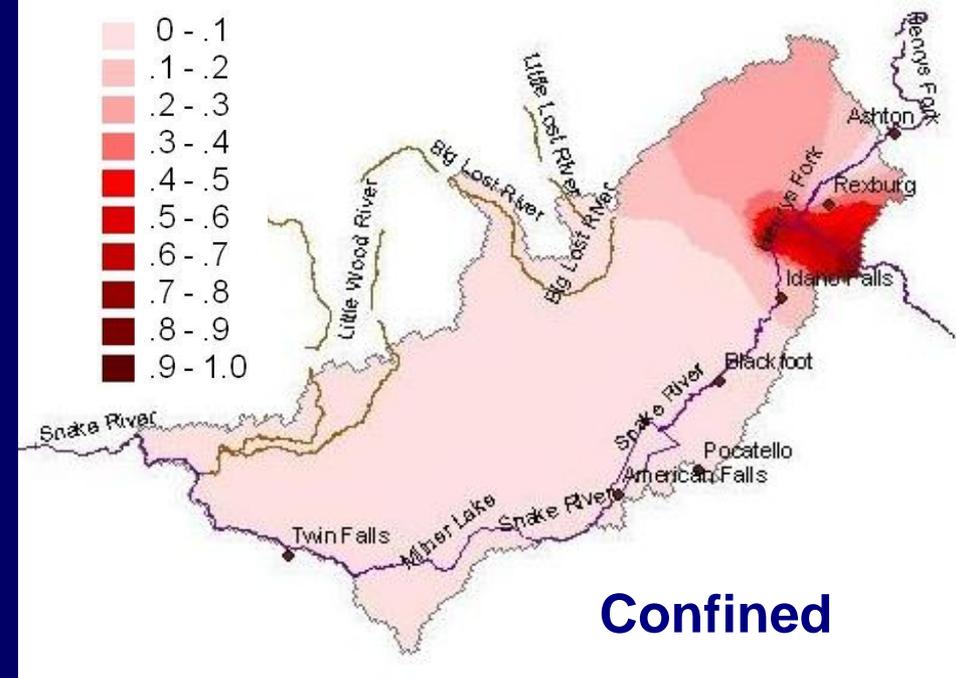
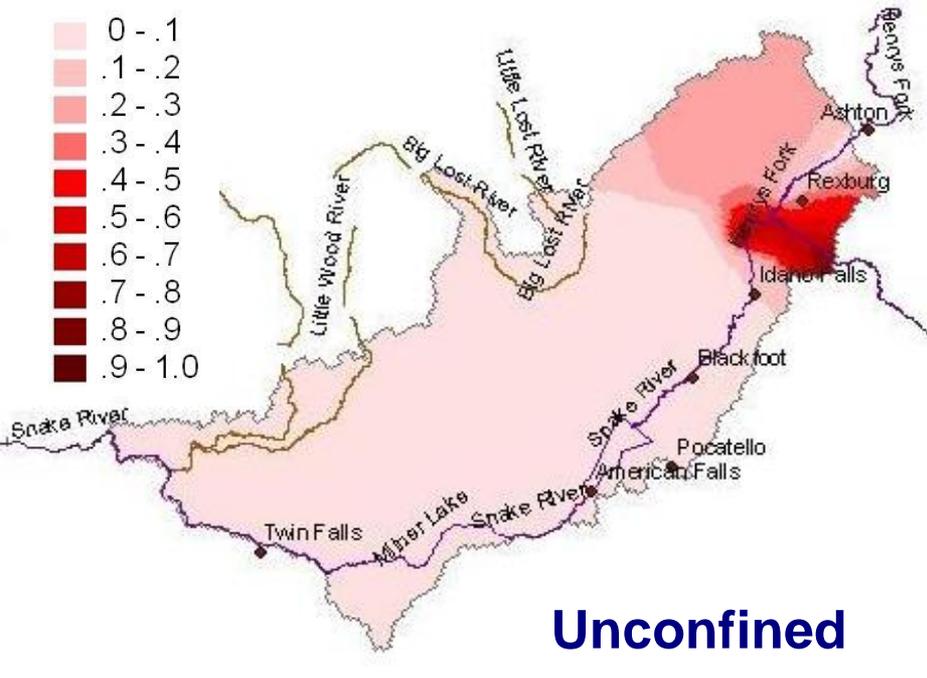
Confined

Unconf - Conf

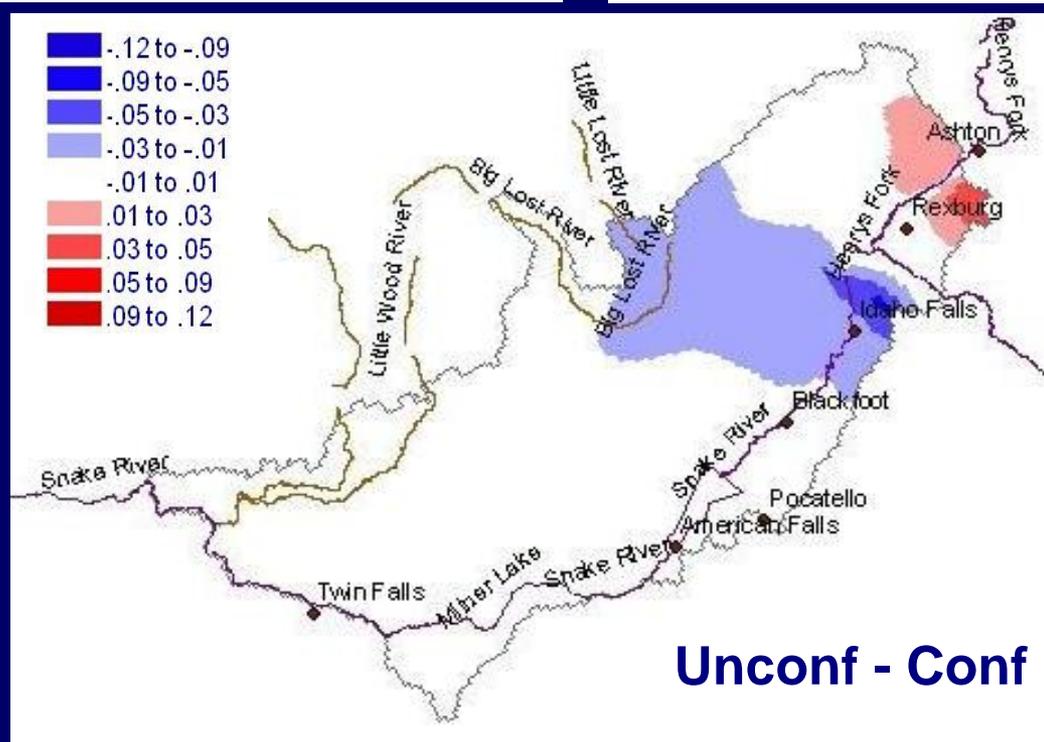


Unconf - Conf

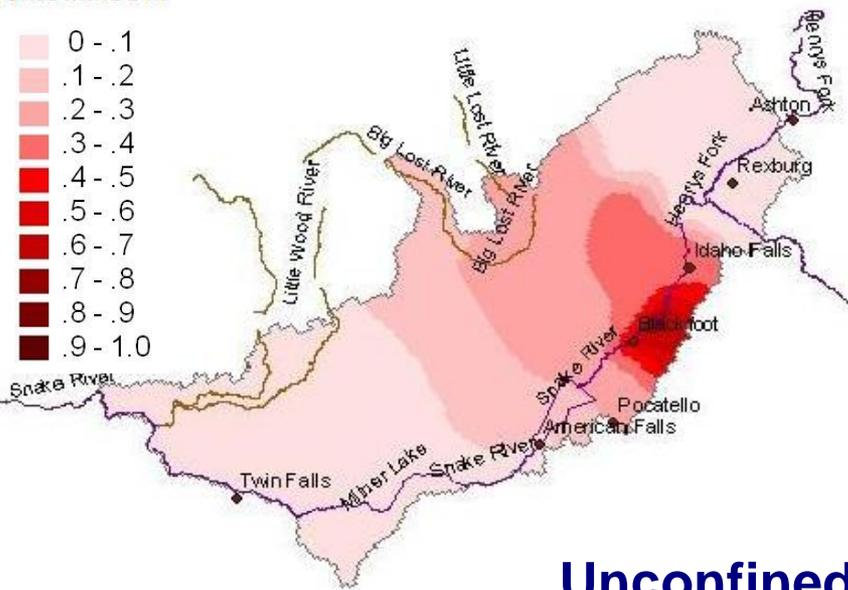
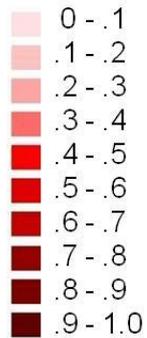
Ashton
To
Rexburg



**Heise
To
Shelley**

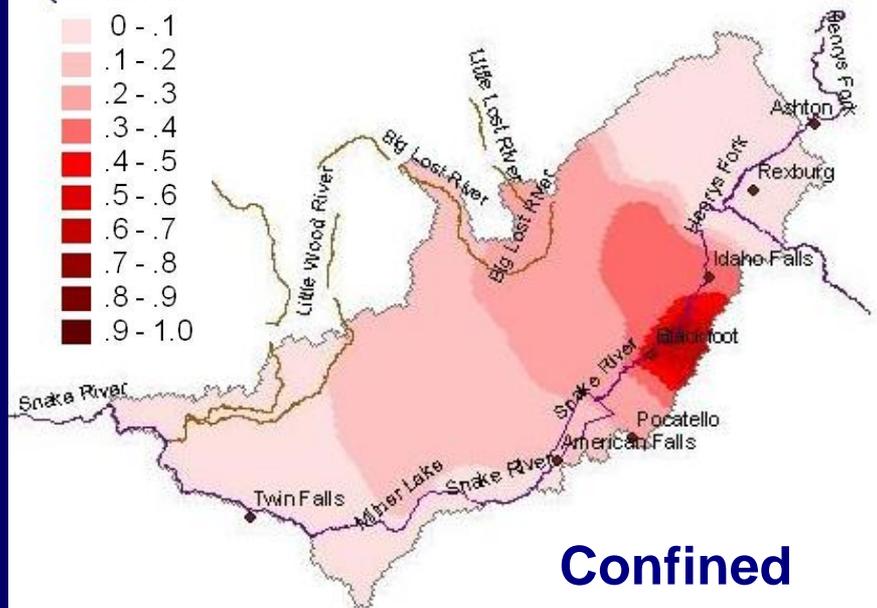
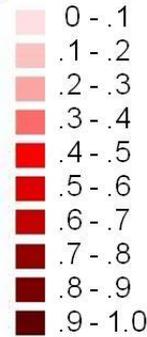


Unconfined RF



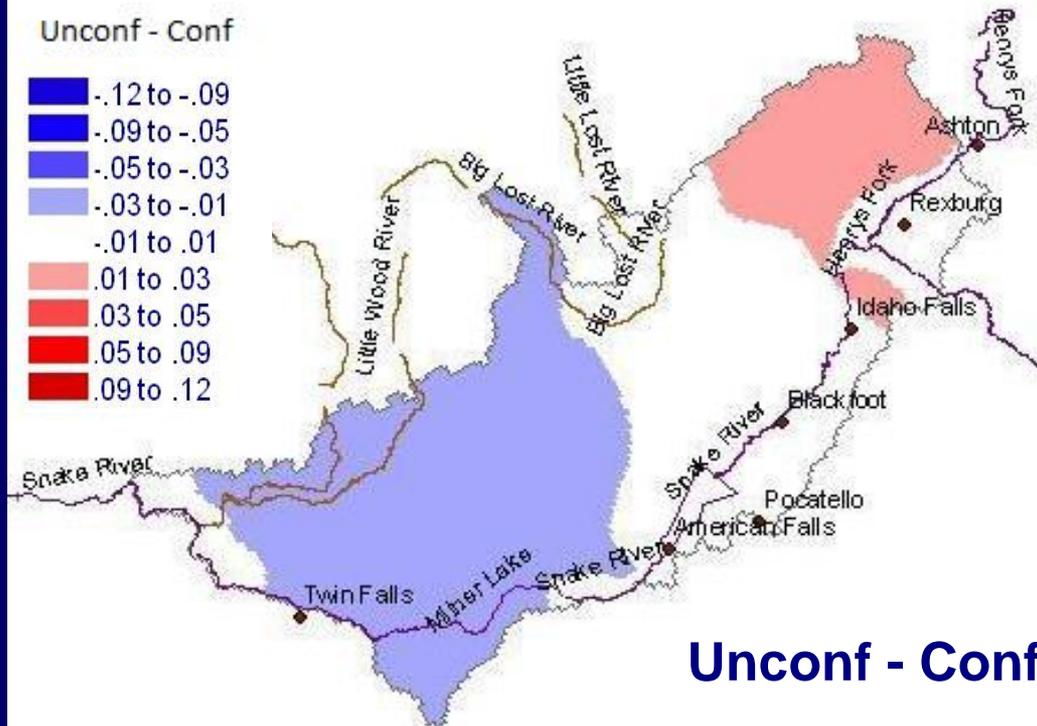
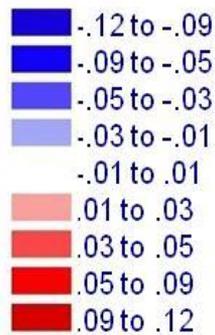
Unconfined

Confined RF



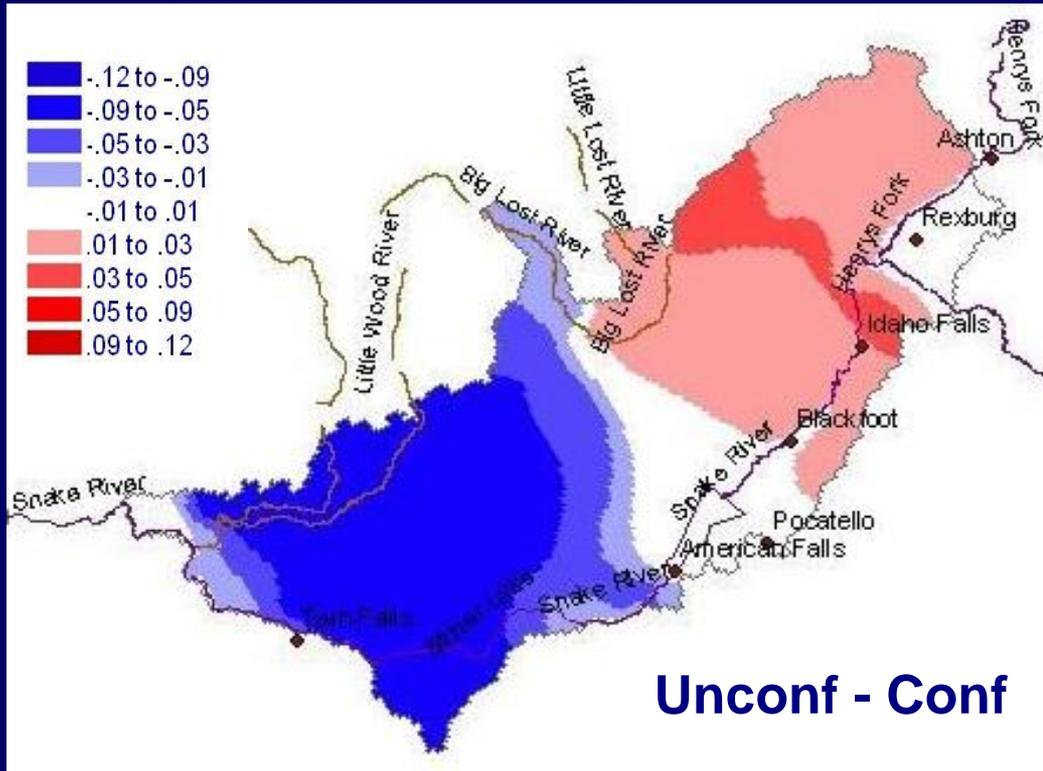
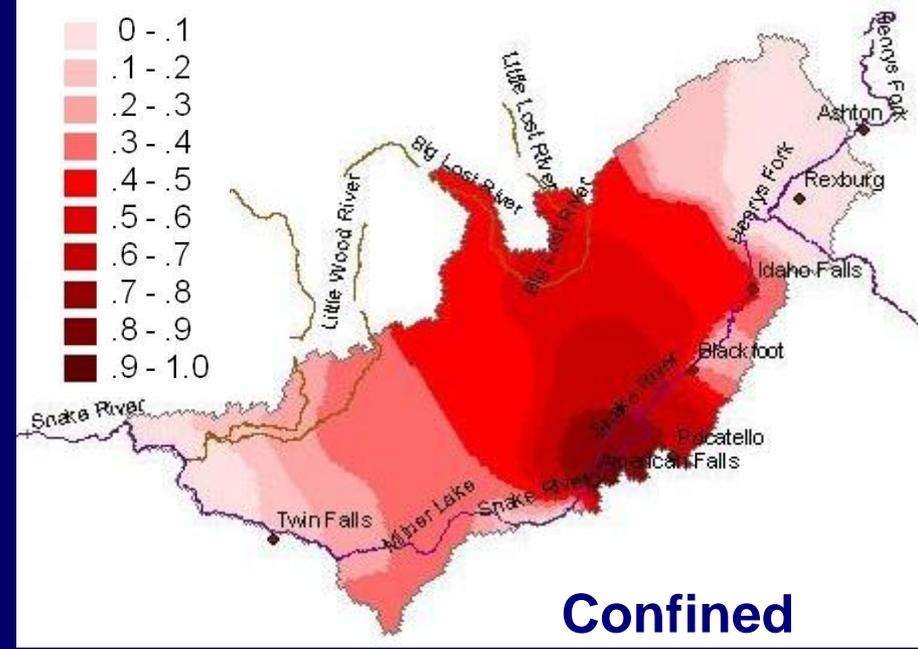
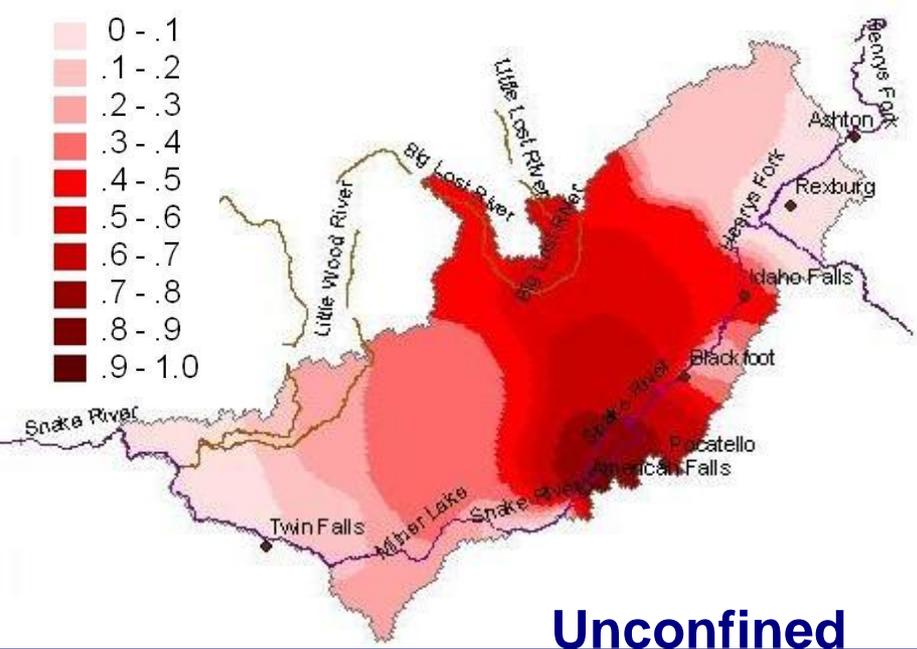
Confined

Unconf - Conf

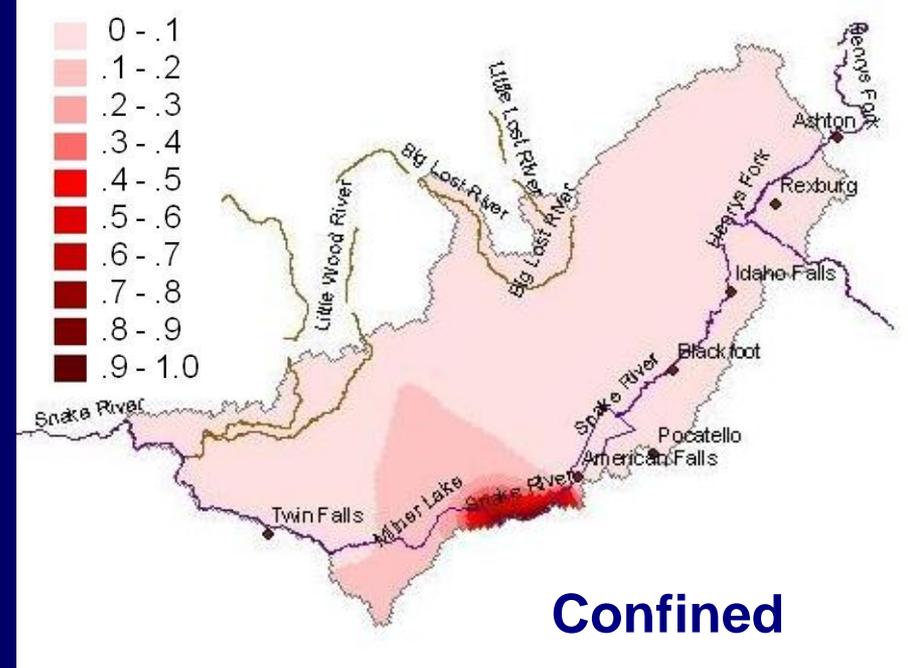
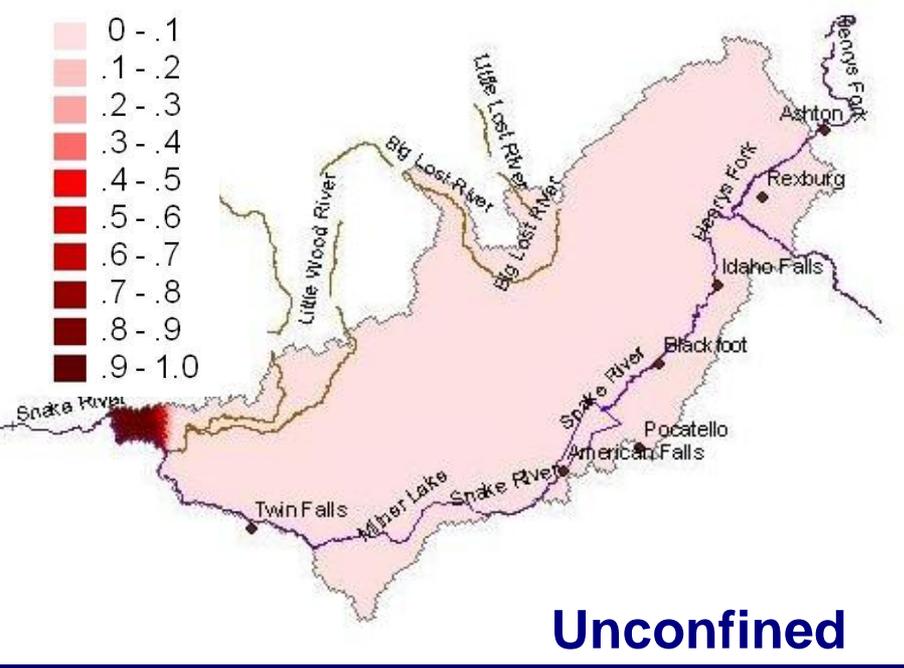


Unconf - Conf

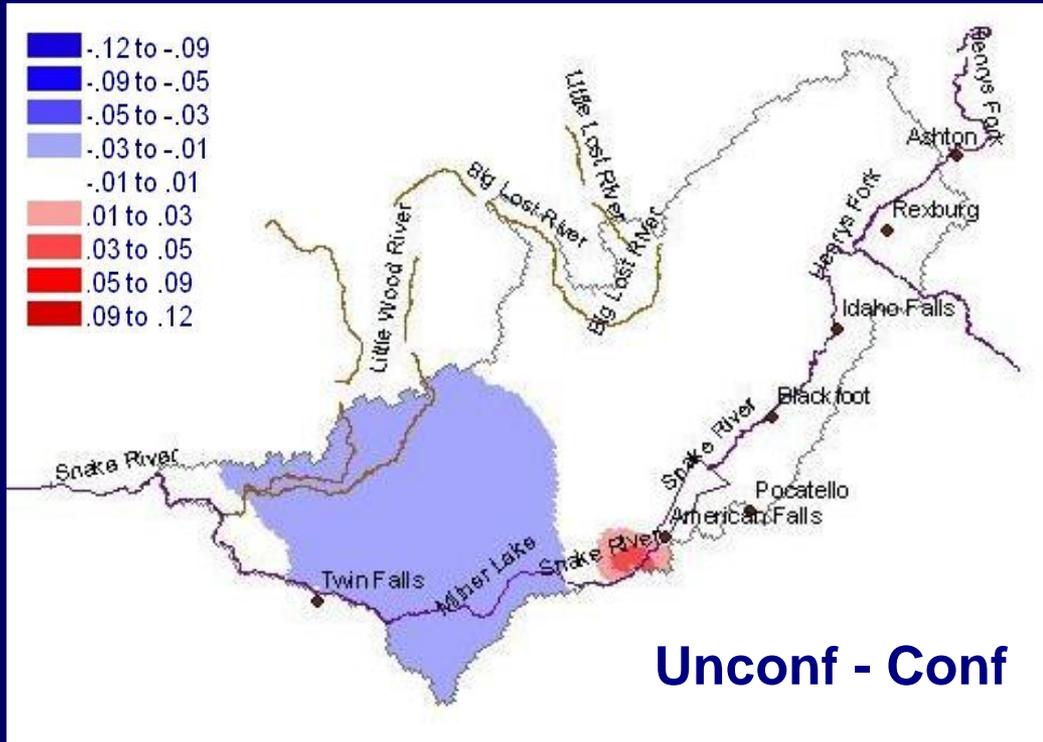
Shelley
To
Blackfoot

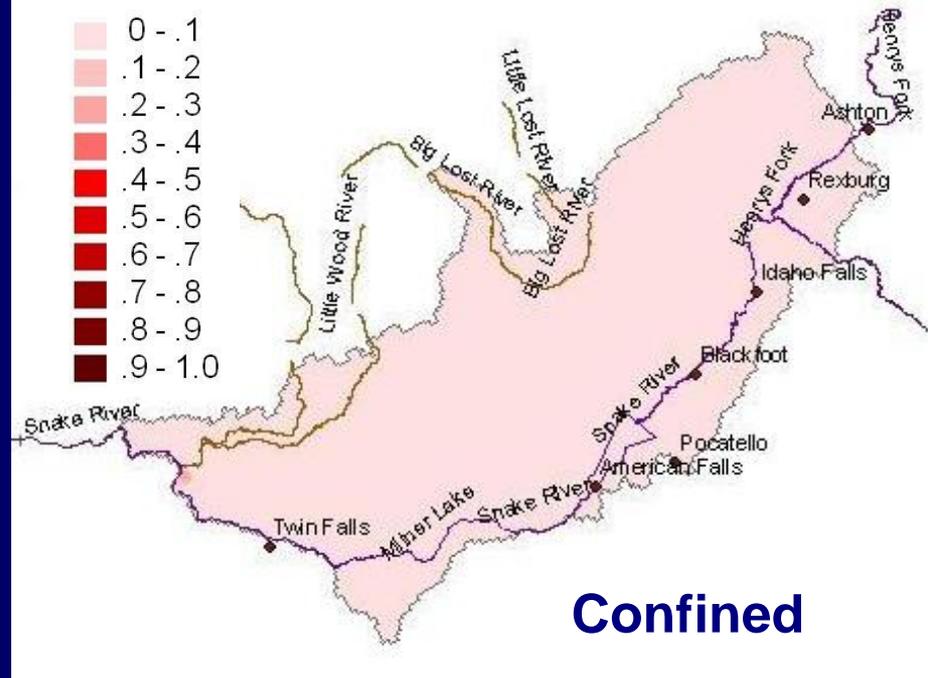
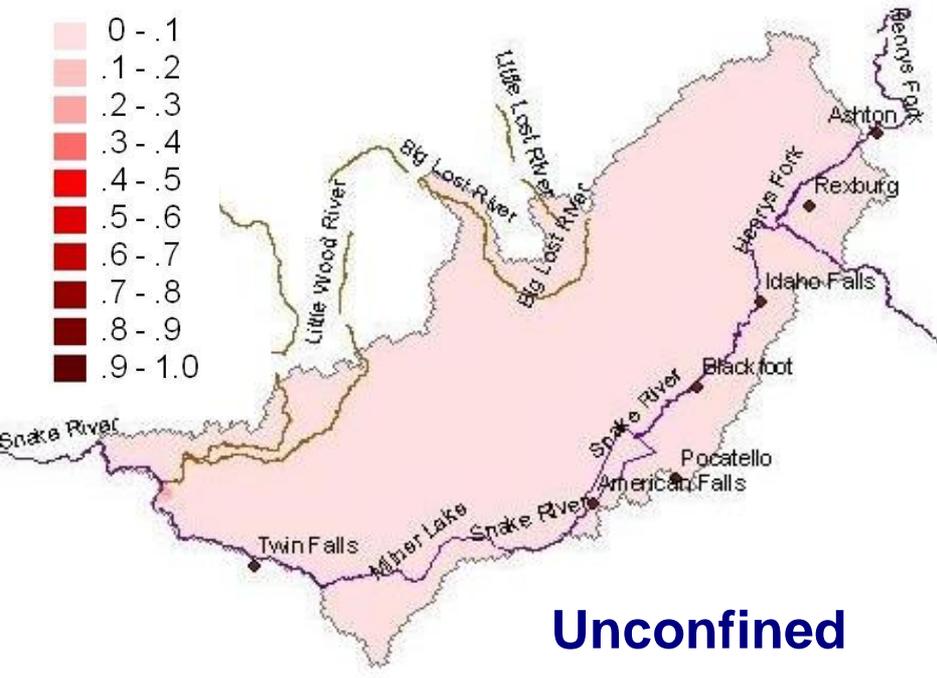


**Blackfoot
 To
 Neeley**

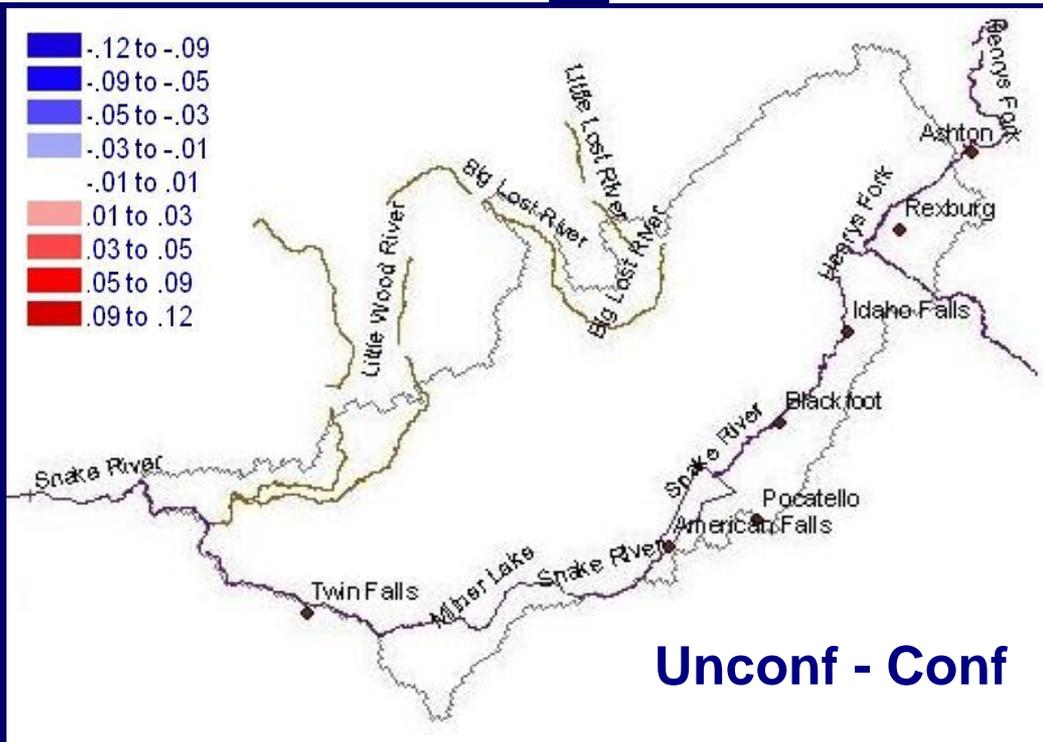


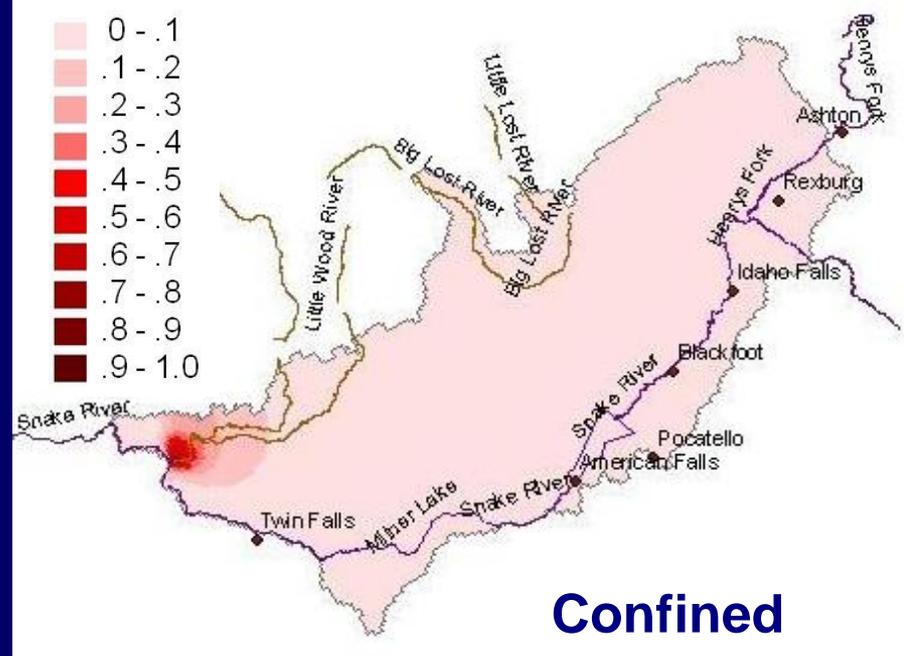
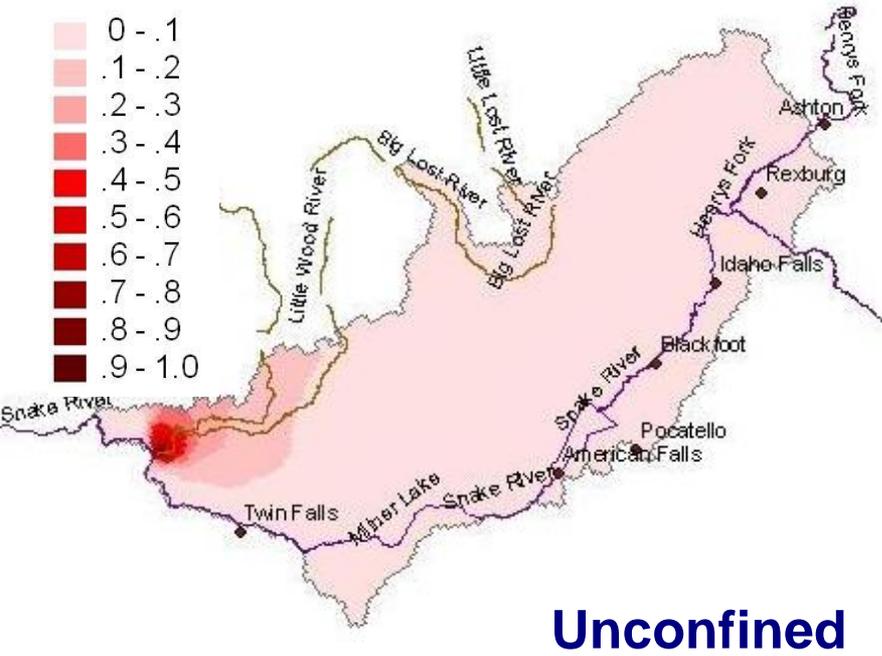
**Neeley
To
Minidoka**



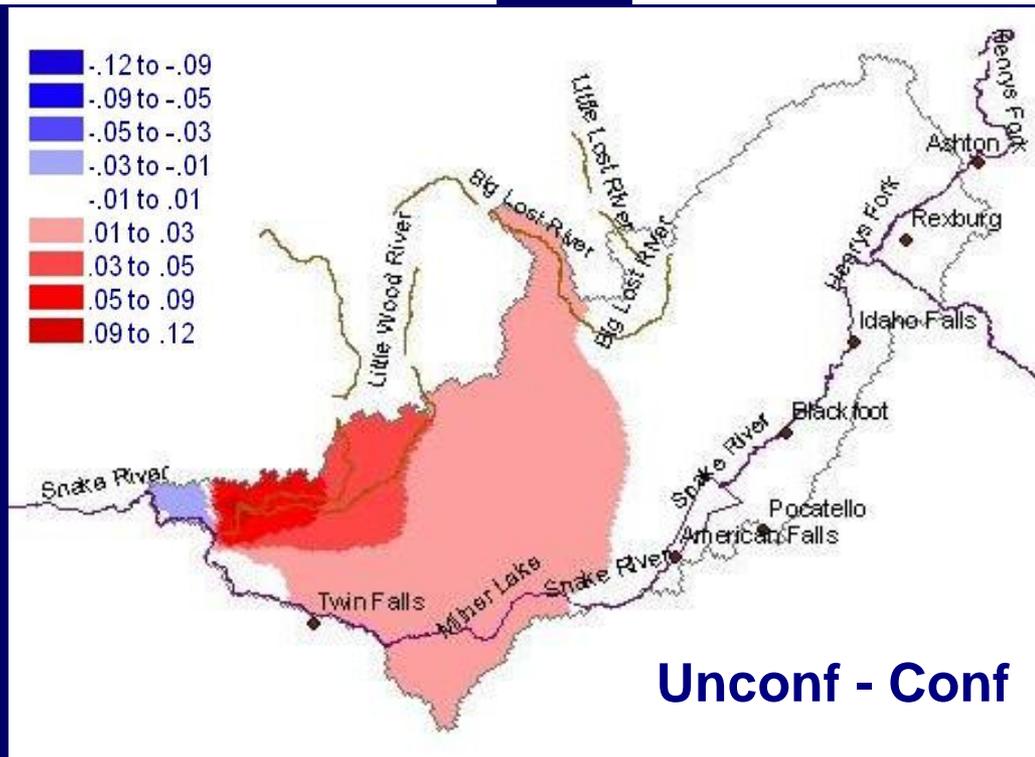


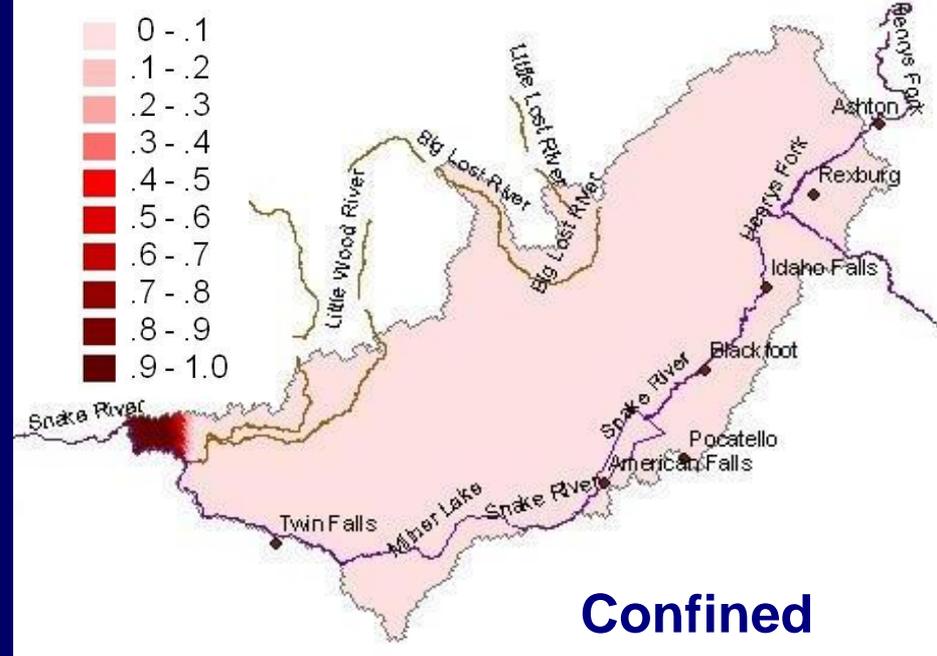
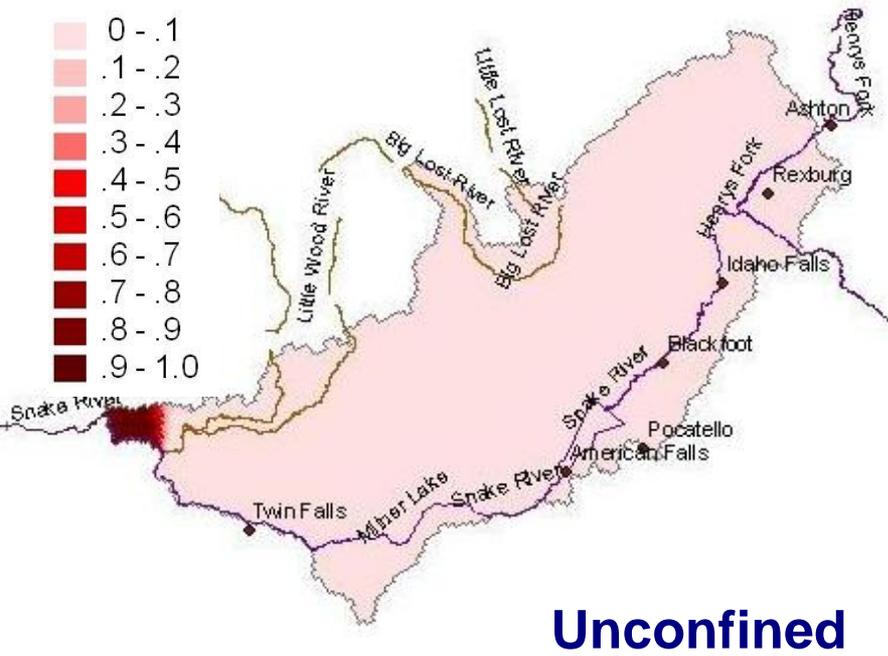
Thousand Springs To Malad



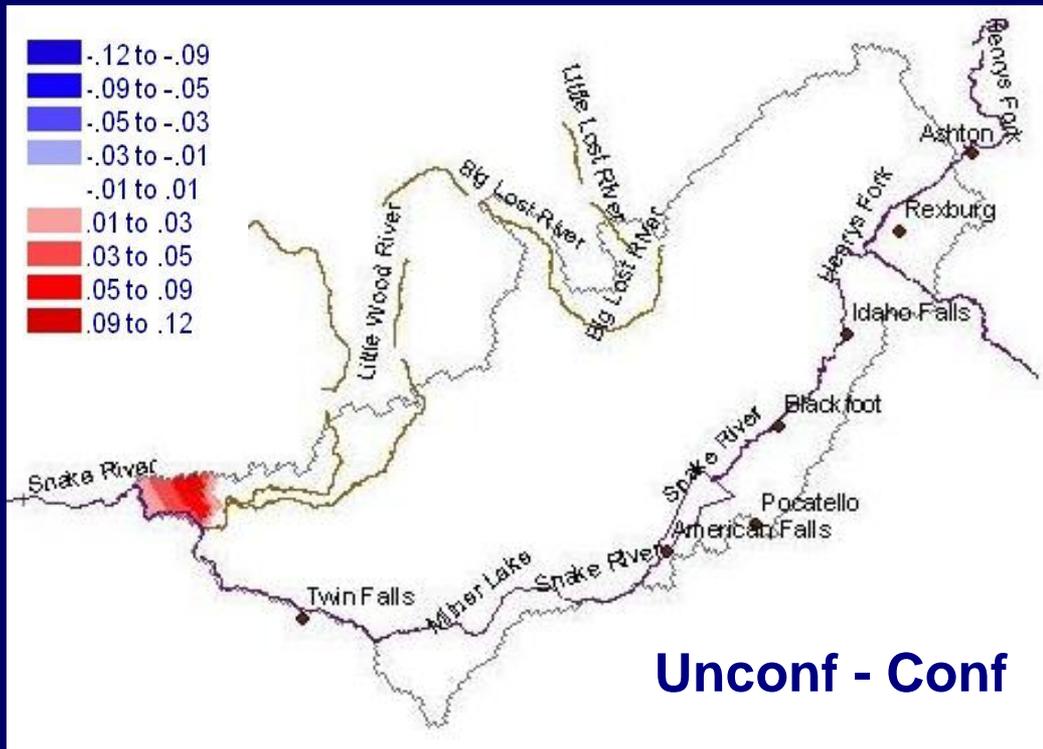


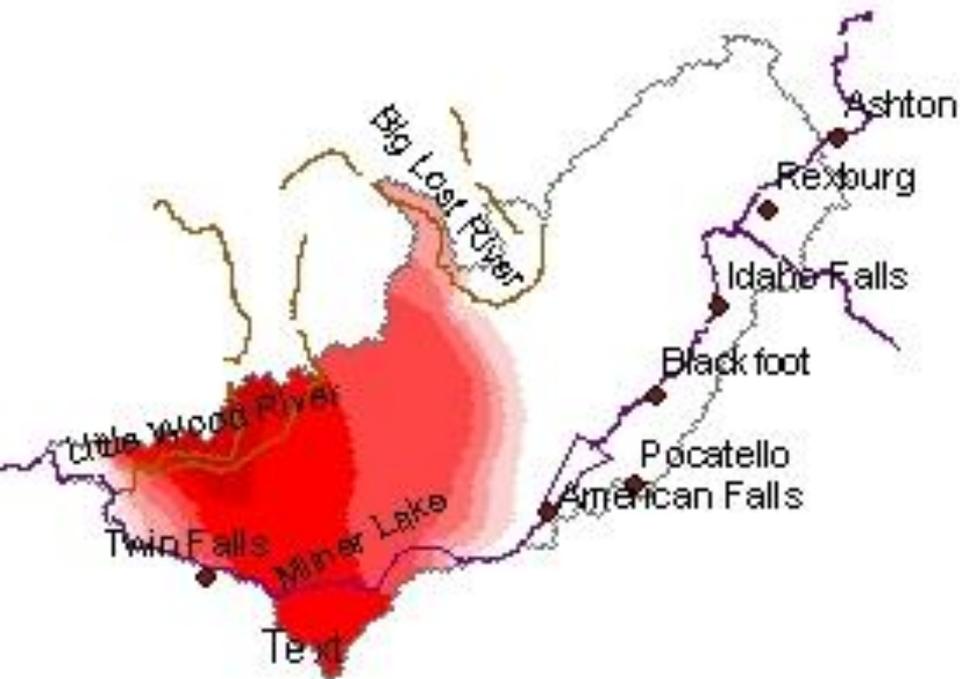
Malad



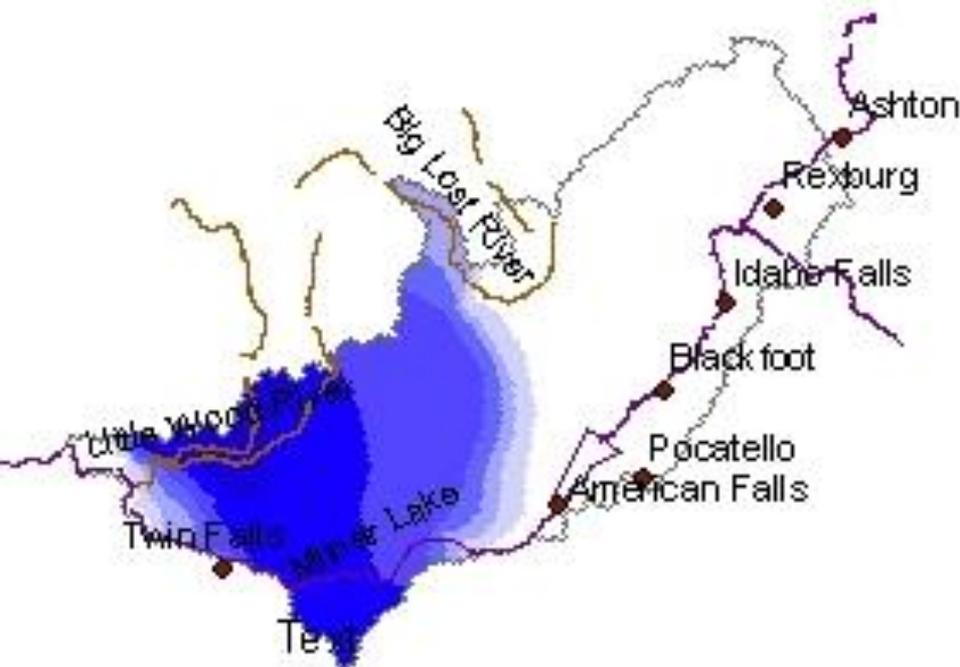


**Malad
 To
 Bancroft**



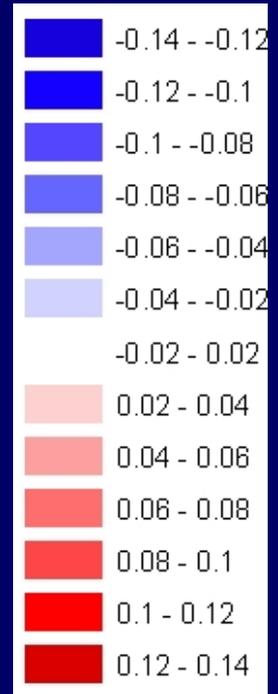


Aggregate Below Milner



Aggregate Above Milner

Unconf RF – Conf RF



Summary

- Unconfined simulations yield larger RFs than confined at down gradient reaches even in thick aquifers
- Results are nearly independent of magnitude or sign of Q
- Difference depends on many factors but can be equivalent to a ΔRF of 0.4 or more (as in Spokane-Rathdrum)
- Differences exist in both transient and SS
- In SRPA, ΔRF is less than 0.12 at all locations and reaches
- MAYBE it doesn't matter because we calibrate under the same conditions as used in applications
- This does not mean that we can't use response functions

Compensating by Calibration?

- Model calibration was as constant thickness and included reach gains
- Did model calibration create artificially large T to lower reaches, compensating for the constant thickness assumption?
 - Difficult to know, but maybe
 - Differences may be small relative to total reach gains but become significant when viewed relative to a specific stress
 - h also used as target which would possibly modify any compensating effect